

Functions Review

Linear Function: A function of the form $y = mx + b$ where m = slope and b = y-intercept.

Example 1: For the equation $6x - 4y = 8$

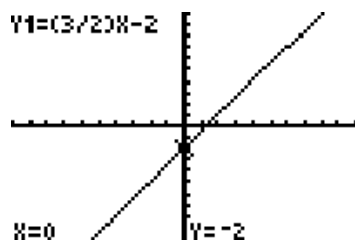
a) Write in the form $y = mx + b$

$$\frac{6x - 8}{4} = \frac{4y}{4}$$

$$y = \frac{6x - 8}{4}$$

$$y = \frac{3x}{2} - 2$$

b) Graph



c) State coordinates of x - intercept

$$(1.3, 0)$$

d) State coordinates of y - intercept

$$(0, -2)$$

e) State slope

$$\frac{3}{2}$$

Quadratic Function: A function of degree 2

Example 2: For the function $y = x^2 - 7x + 10$

a) Graph

b) State the coordinates of the vertex

$$(3.5, -2.25)$$

c) State the max/min values

$$-2.25$$

d) State the equation of axis of symmetry

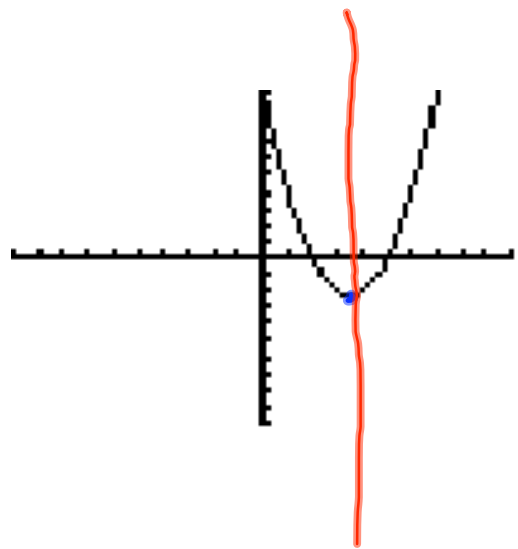
$$x = 3.5$$

e) State the coordinates of x-intercepts

$$(2, 0) \quad (5, 0)$$

f) State the coordinates of y-intercept

$$(0, 10)$$



Cubic Function: A functions of degree three

Example 3: For the function $y = -3x^3 - 8x^2 - 3$

a) Graph

b) State the coordinates of relative max/min points

rel. min: $(-1.8, -11.4)$

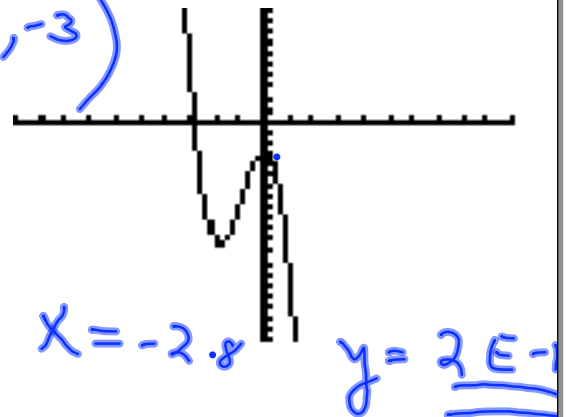
rel. max: $(0, -3)$

c) State the coordinates of zeros

$(-2.8, 0)$

d) State the coordinates of y - intercept

$(0, -3)$



Absolute Value Function: A function with a variable within the absolute value symbol.

Example 4: For the function $y = |2x - 1| - 3$

a) Graph

b) State the coordinates of the vertex

$$(0.5, -3)$$

c) State the domain and range

$$D: x \in \mathbb{R} \quad R: y \geq -3$$

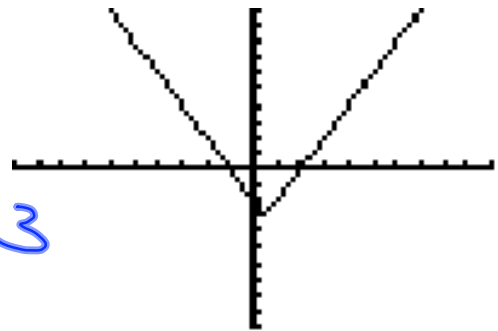
d) State the equation of the axis of symmetry

$$x = 0.5$$

e) State all intercepts

$$\underline{x\text{-int}} \quad (-1, 0) \\ (2, 0)$$

$$\underline{y\text{-int}}: (0, -3)$$



Radical Functions: A function that has a variable in the radicand.

Example 5: For the function $y = \sqrt{x+11} - 15$

- Graph
- State window settings to be able to see x and y - intercepts
- State domain and range
- State all intercepts

Window Settings

$$X: \overset{x_{\min}}{-5}, \overset{x_{\max}}{1}, \overset{x_{\text{sc}}}{1}$$

$$Y: [-13, -11, 0.5]$$

Algebraically finding x & y - units

y-int:

$$y = \sqrt{x+11} - 15$$

Substitute $x = 0$

$$y = \sqrt{0+11} - 15$$

$$y = -11.68$$

x-int

$$y = \sqrt{x+11} - 15$$

$$0 \overset{+15}{=} \sqrt{x+11} - 15 \overset{+15}{+15}$$

$$(15)^2 = (\sqrt{x+11})^2$$

$$225 = x + 11$$

$$x = 214$$

Rational Function: A function of the form $f(x) = \frac{g(x)}{h(x)}$ where $g(x)$ and $h(x)$ are polynomials and $h(x)$ not equal to zero.

Asymptote: A line that a curve approaches more and more closely.

Example 6: For the function $y = \frac{-3x}{x-1}$

- a) Graph
- b) State the vertical and horizontal asymptotes
- c) State the domain and range