

## Day 2: Graphing Circles and Rectangular Hyperbolas

\*\*CONICS program for calculators

Handout Investigation

Wolframalpha.com

### General Form Conics

$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

$$4x^2 + 4y^2 - 35 = 0 \quad \text{circle } \odot$$

Circle Both +ve

$$A = C$$

Ellipse Both +ve

$$A \neq C$$

Parabola One of A or C but not both.

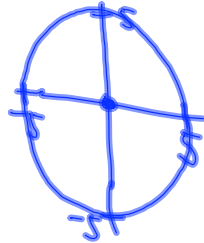
Hyperbola Opposite signs

Investigate:

1) Pg. 527 #1-2

The Equation  $x^2 + y^2 = r^2$ 

$$x^2 + y^2 = 25$$

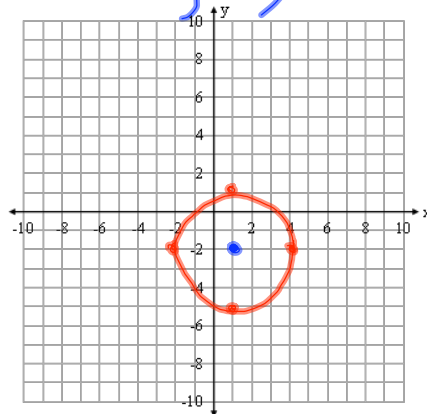
radius 5  $\uparrow$  radius

Handout Investigation I - III

The Equation  $(x-h)^2 + (y-k)^2 = r^2$ 

$$(x-1)^2 + (y+2)^2 = 9$$

$(h,k)$  center  $r = \text{radius}$

Center  $(1, -2)$   $r = 3$ 

Investigation Pg. 528 4-7

The Equation  $x^2 - y^2 = r^2$

Eg.  $x^2 - y^2 = 9$

Since  $x^2$  is positive it tells us that the hyperbola opens along the x - axis. The coordinates of the vertices are (-3, 0) and (3,0) found by taking the square root of the constant term.

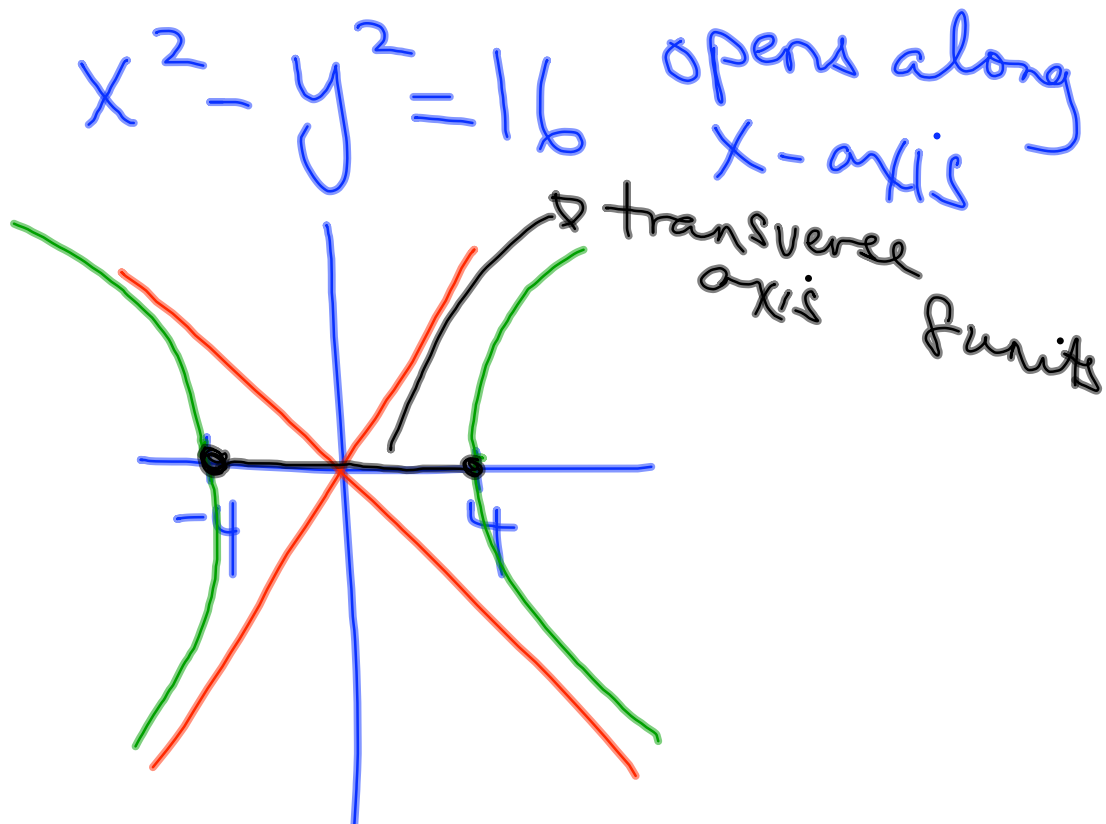
The Equation  $x^2 - y^2 = -r^2$  or  $y^2 - x^2 = r^2$

(4,5)

Eg.  $x^2 - y^2 = -9$  becomes  $y^2 - x^2 = 9$

Since  $y^2$  is positive it tells us that the hyperbola opens along the y - axis. The coordinates of the vertices are (0, -3) and (0, 3) found by taking the square root of the constant term.

**These hyperbolas have asymptotes of  $y = x$  and  $y = -x$ .** The line segment joining the vertices is called the **transverse axis**. In the previous examples the length of that segment is 6 units.



**Assignment:**  
**Pg. 532 1-4, 9, 10**