

Day 4: Translating Graphs of Conics

Describe the effect of h and k on

$$(x-h)^2 \text{ and } (y-k)^2$$

If you have trouble, think of this example:

$$(x-2)^2 + (y+5)^2 = 1$$

$(h, k) \rightarrow$ center of my conic is .

**h moves the graph left or right, while k moves the graph up or down. Therefore, (h, k) represents the location of the centre of the conic.

Steps for sketching ANY conic from its equation:

- 1) Decide on the type of conic from the equation
- 2) Locate the centre
- 3) Depending on the type of conic:
 - a) Plot the major/minor axis (ellipse/circle)
 - b) Plot the asymptotes/transverse axis (hyperbola)
- 4) Plot the vertices and sketch the graph

The expectations for EXACTLY the amount of work necessary to describe and sketch a conic given its equation will be demonstrated with the following examples. You MUST show all of this work for each individual conic type to earn full credit for a problem.

Eg 1) Describe and sketch the conic represented by

$$\frac{(x-2)^2}{16} + \frac{(y+3)^2}{9} = 1$$

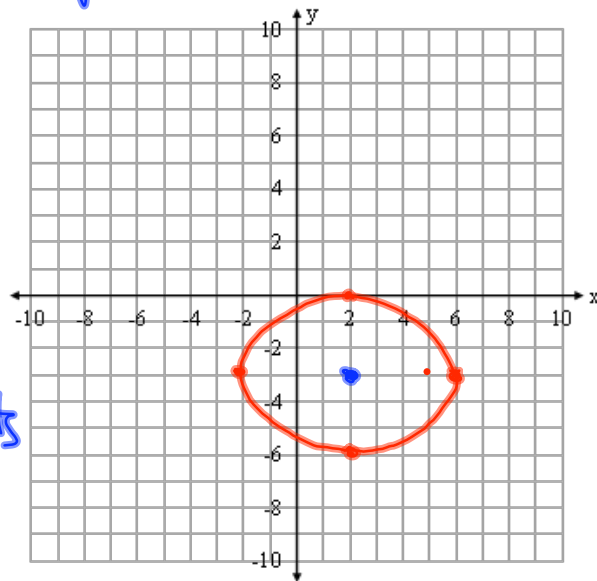
ellipse

Center: (2, -3)

Major axis: 4 units

To the right & left of center.
8 unit

Minor axis: 6 units



$x+1=0$
 $x=-1$
Eg 2) Describe and sketch the conic represented by

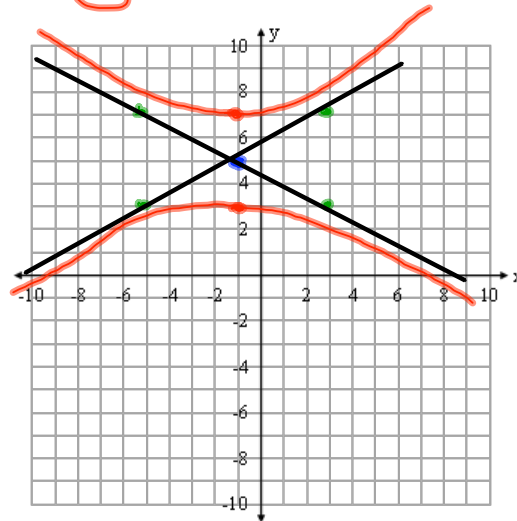
$$-\frac{(x+1)^2}{16} + \frac{(y-5)^2}{4} = +1$$

Center: $(-1, 5)$

vertices: $(-1, 7)$
 $(-1, 3)$

asymptotes:
 $y = \pm \frac{2}{4}x$

Hyperbola



Eg 3) Describe and sketch the conic represented by

parabola open to the right.

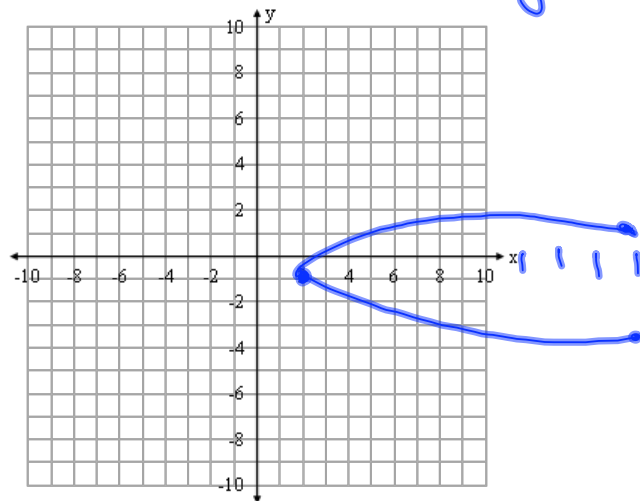
$$x-2 = 3(y+1)^2$$

$$x = 3(y+1)^2 + 2$$

Vertex: $(2, -1)$

$$x = 3(1+0)^2 + 2$$

$$\underline{x = 14} \quad (14, 1)$$



Assignment:
Pg. 548 #3-5, 6a-b

odds